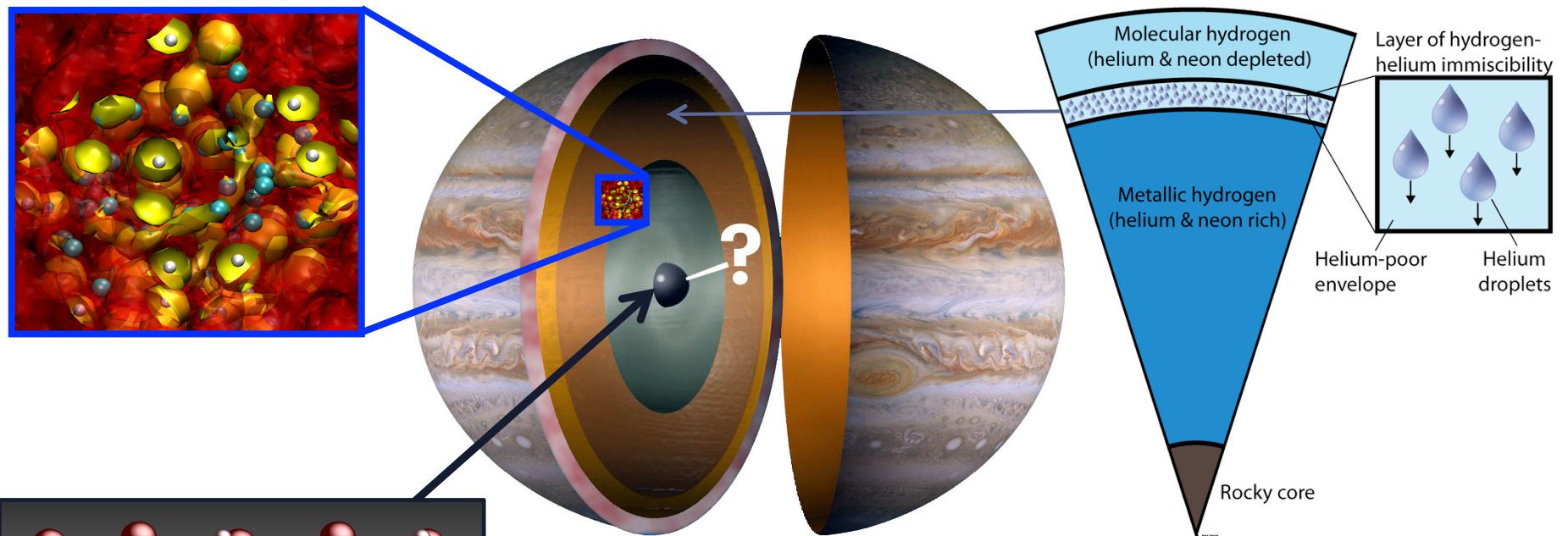


Phase Separation in Giant Planet Interiors and Novel First-Principles Simulation of Plasmas



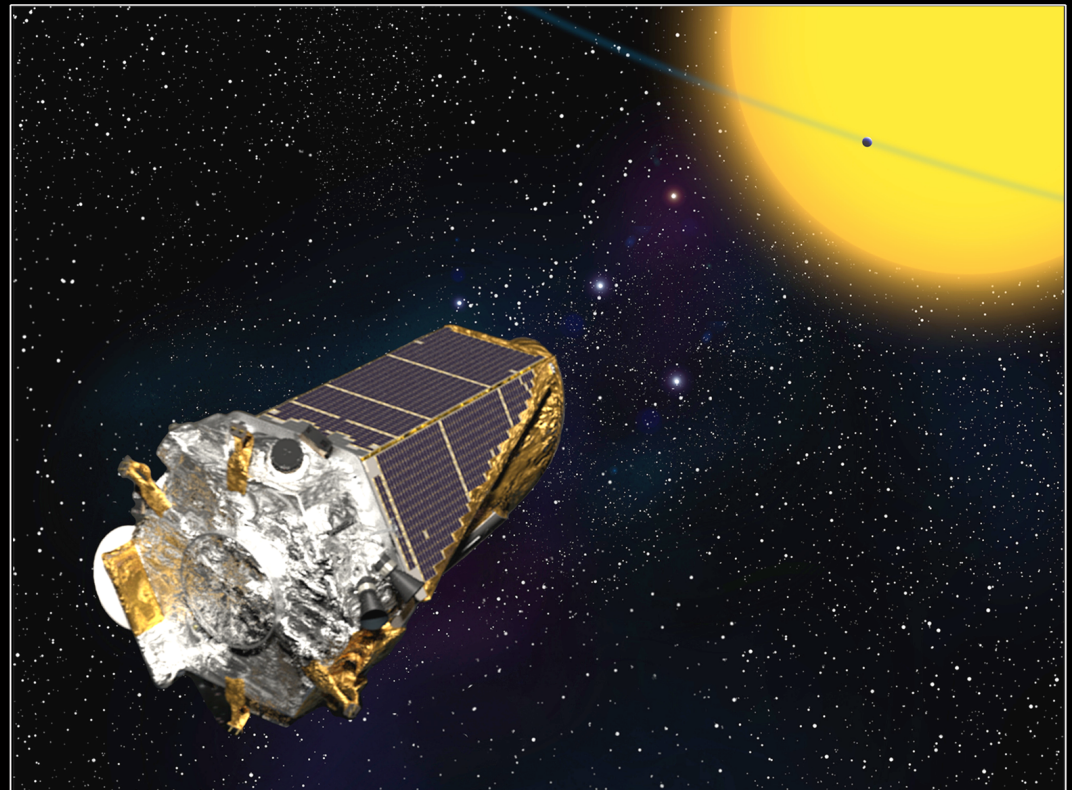
**Burkhard Militzer,
Kevin Driver, Hugh Wilson**

UC Berkeley

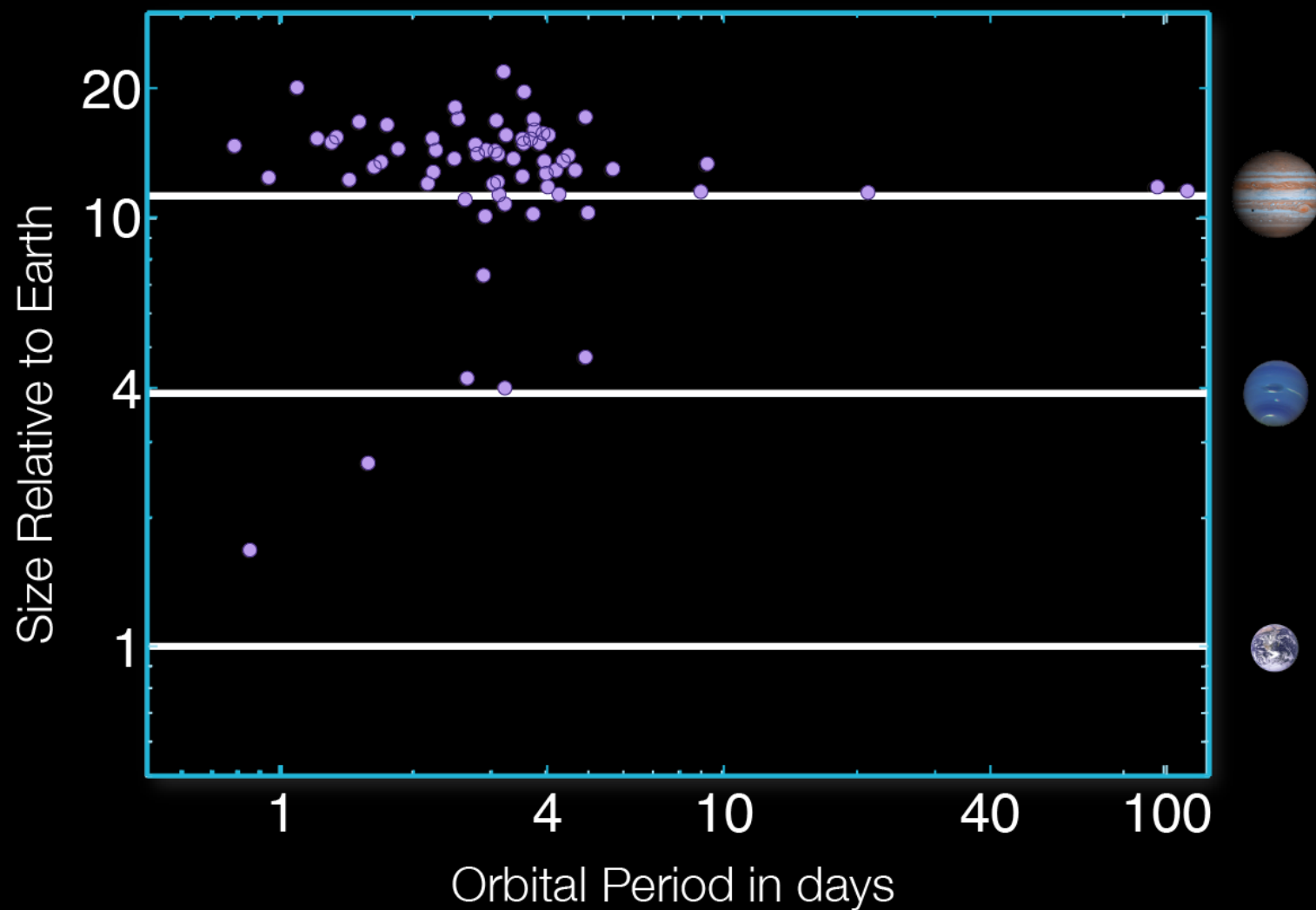
<http://militzer.berkeley.edu>

NASA's Kepler Mission

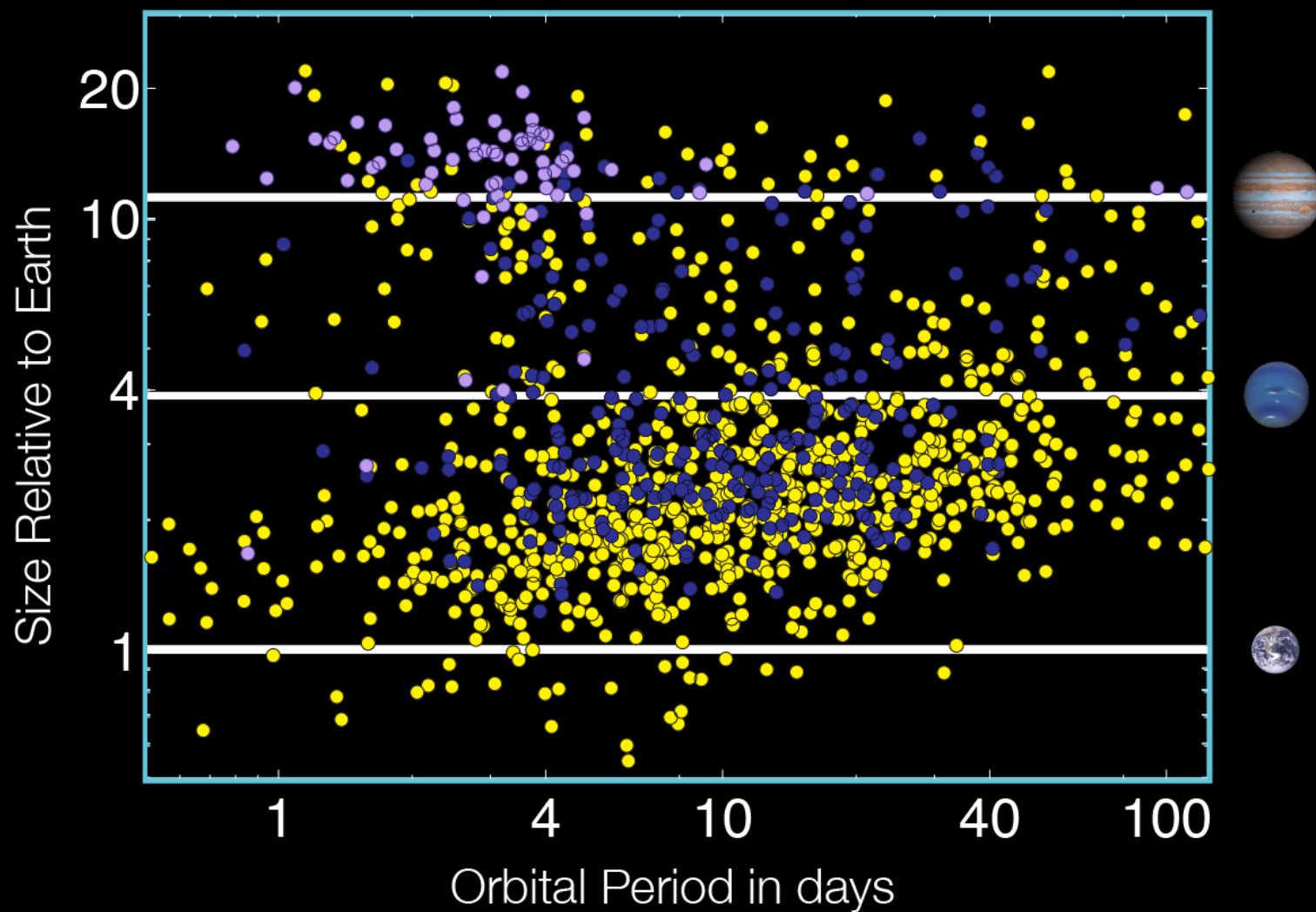
- Determine the frequency of Earth-size and larger planets in the habitable zone of sun-like stars
- Determine the size and orbital period distributions of planets



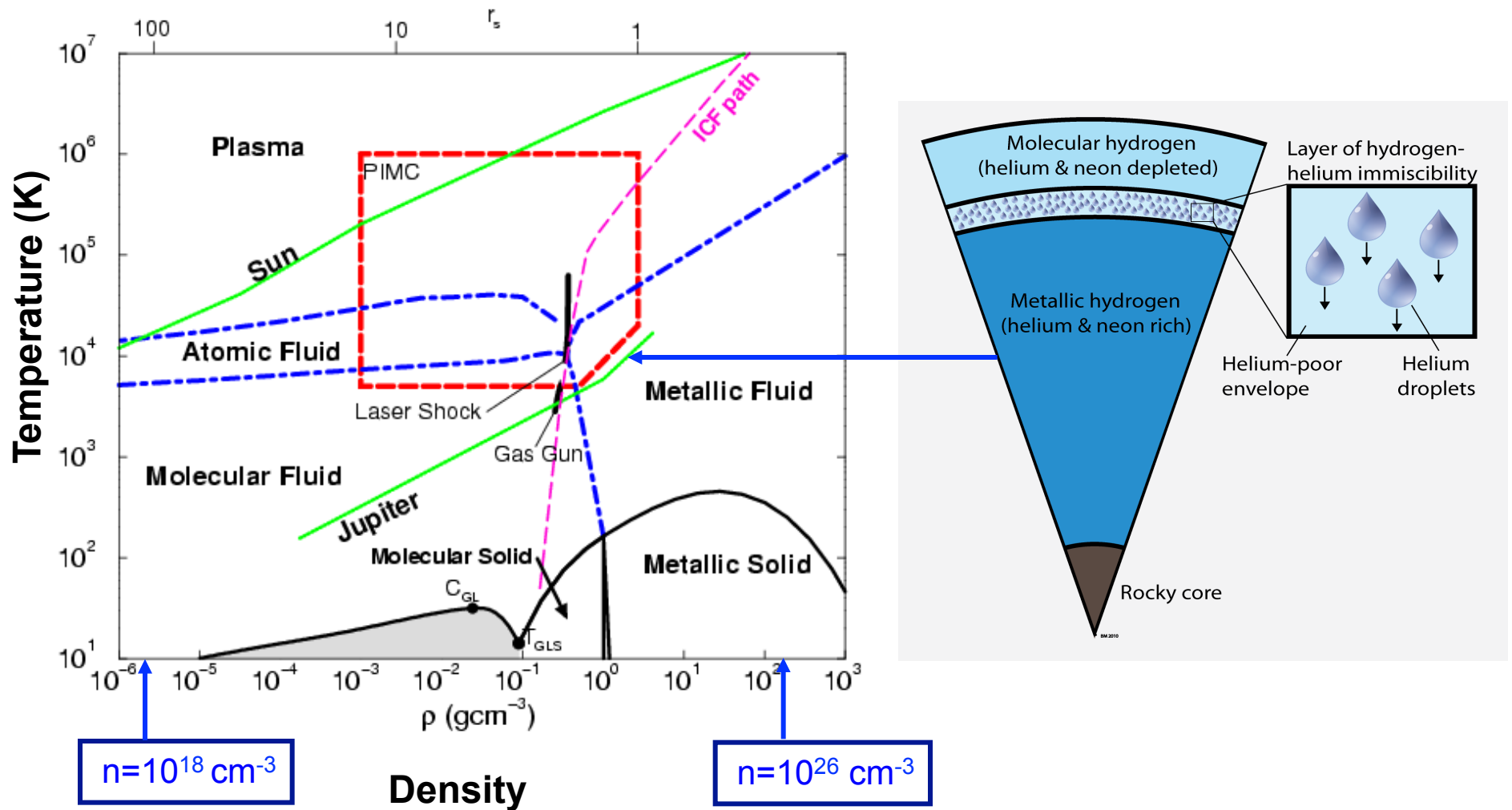
Pre-Kepler Transiting Planets - 2009



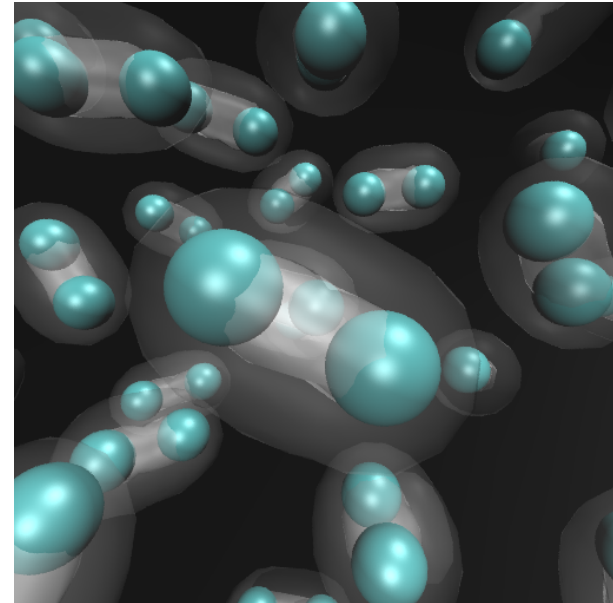
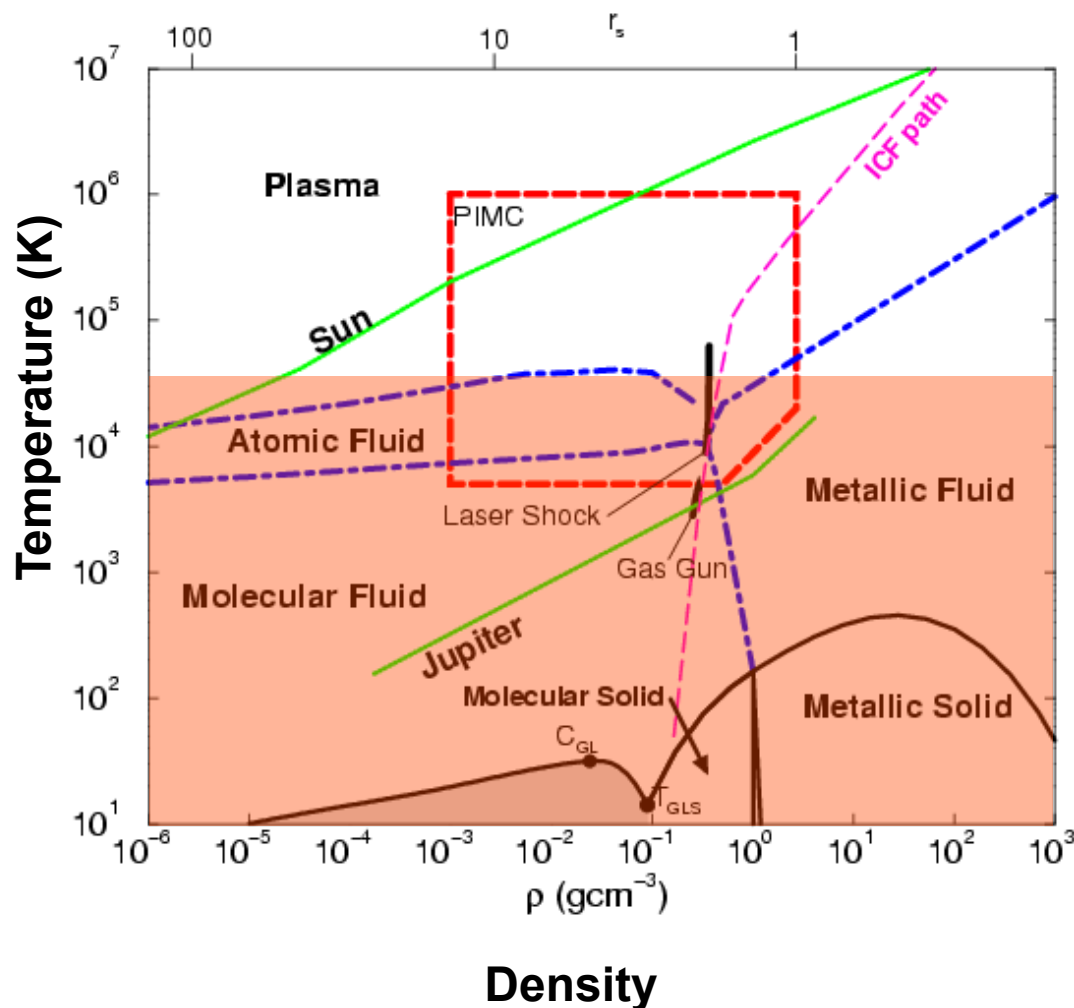
Kepler Candidates as of February 1, 2011



Ab initio Simulations to Characterize of the Interiors of Giant Planets



1) Density functional molecular dynamics

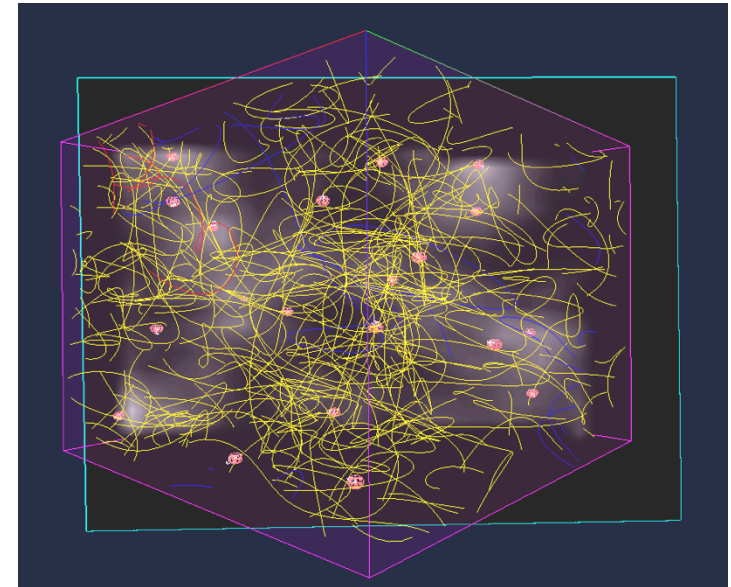
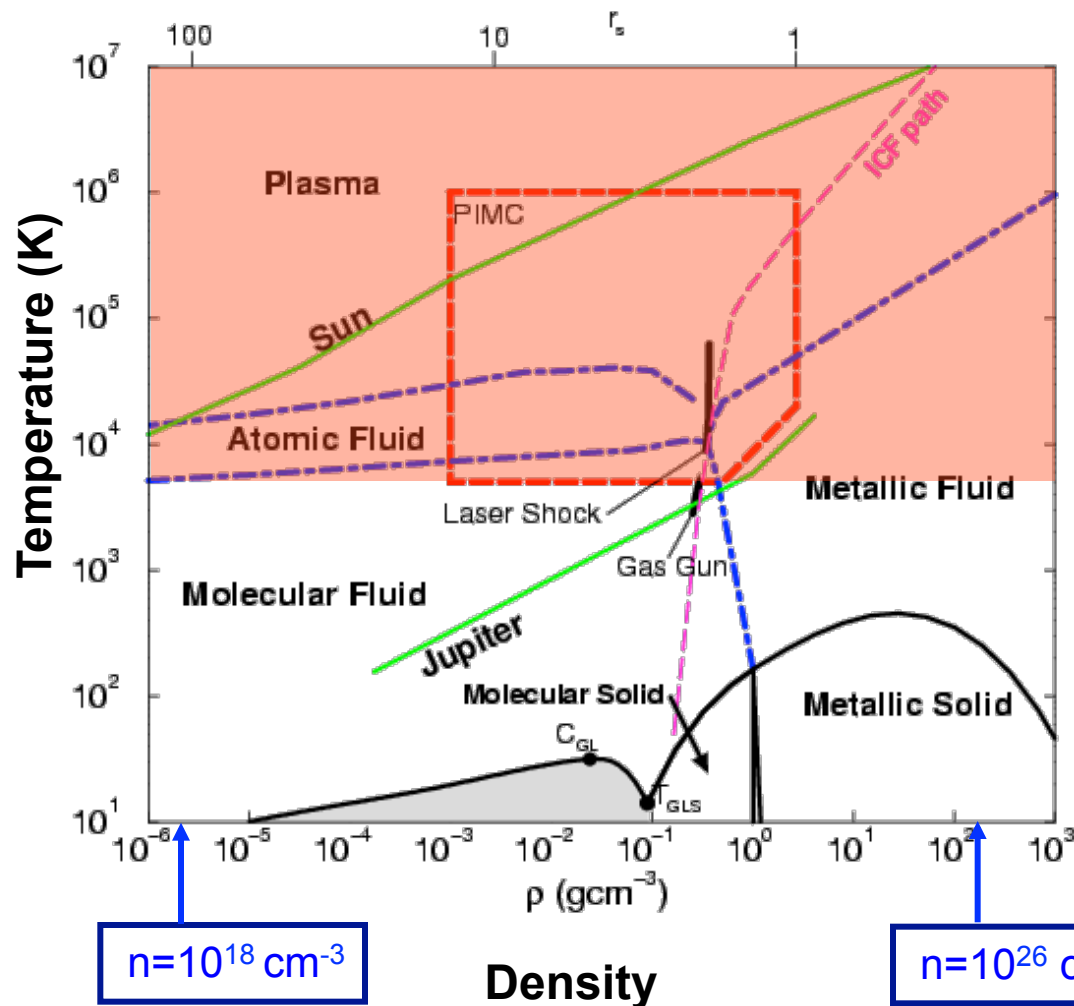


Born-Oppenheimer approx.
MD with classical nuclei:

$$\mathbf{F} = m \mathbf{a}$$

Forces derived DFT with
electrons in the instantaneous
ground state.

- 1) Density functional molecular dynamics
- 2) Path integral Monte Carlo for higher temperatures



PIMC applicable at:
 $T > 5000\text{K}$



2012 Summer School on Computational Materials Science Quantum Monte Carlo: Theory and Fundamentals

July 23-27, 2012 • University of Illinois at Urbana-Champaign

Topics:

- Introduction to Monte Carlo Methods • Pseudopotential generation
- Variational Quantum Monte Carlo • Diffusion Quantum Monte Carlo
- Wavefunction optimization methods • Path integral Monte Carlo
- QMC applications in geophysics

Details:

Scientists from geophysics, physics, materials science, chemistry and high-performance computing. Includes lectures and labs.

\$150 registration fee. Housing provided for non-local participants.

Application deadline: **June 11, 2012**

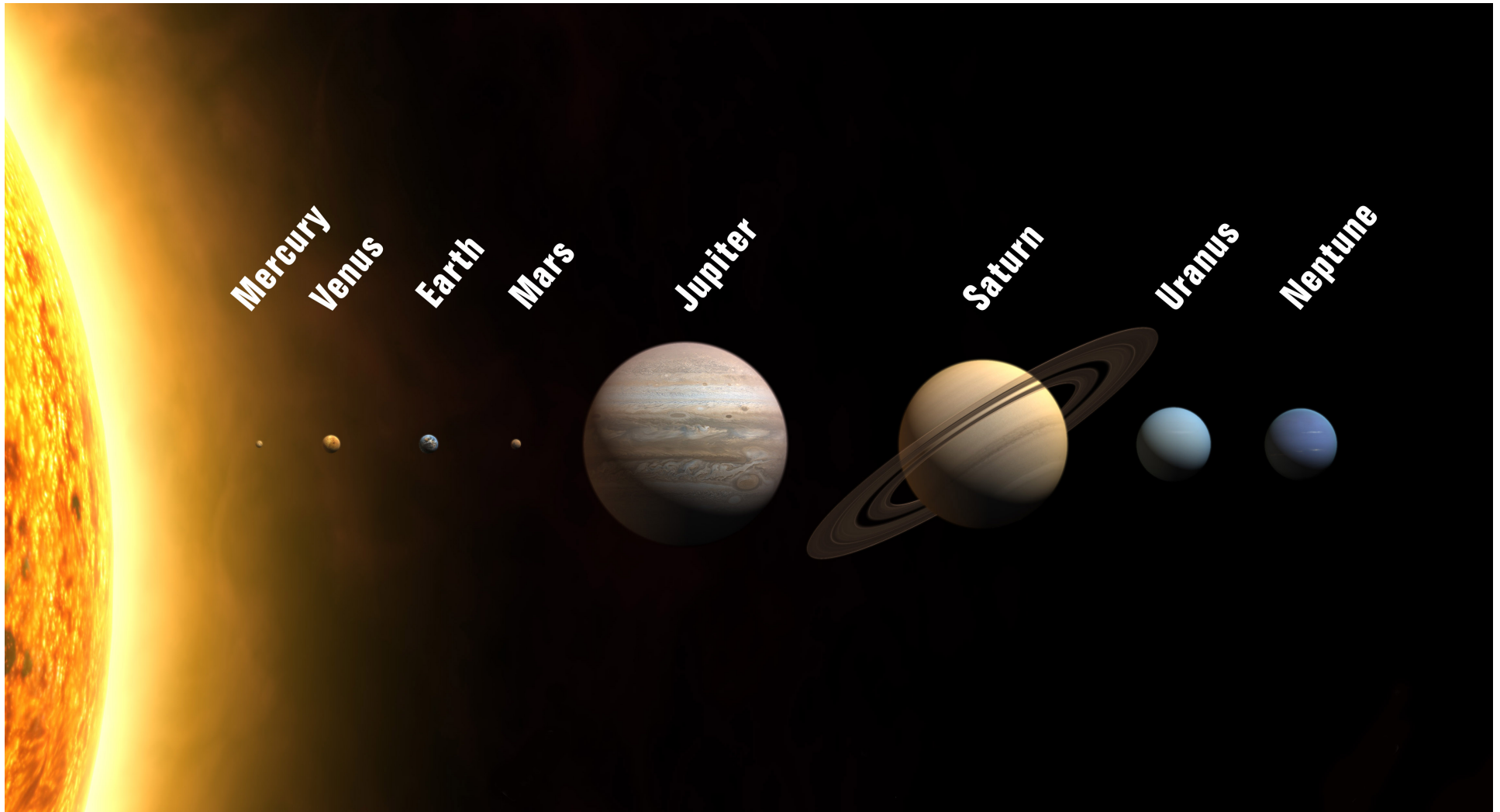
Contact: <http://mcc.illinois.edu/summerschool/2012>

Email: mcc-workshops@illinois.edu

Organizers:

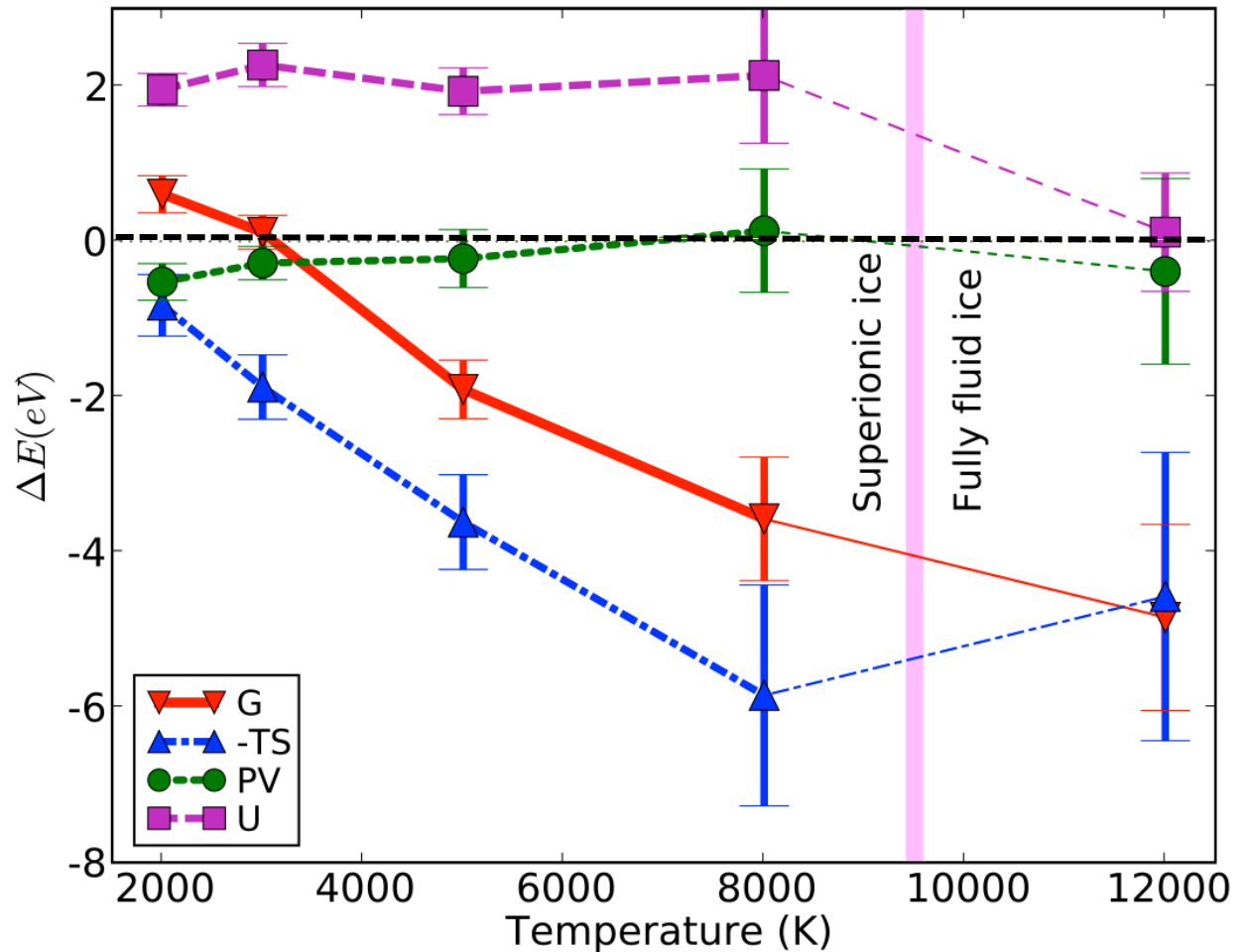
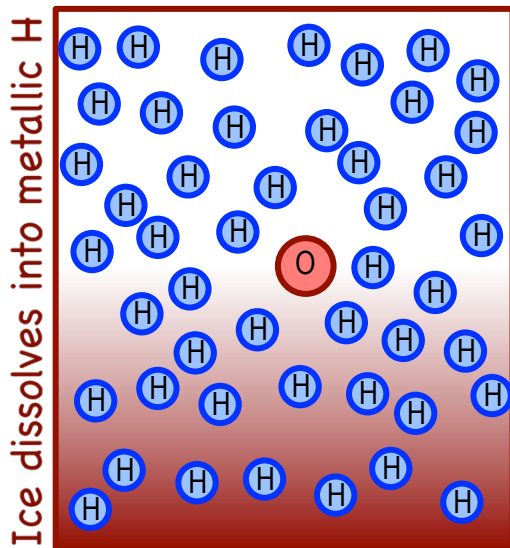
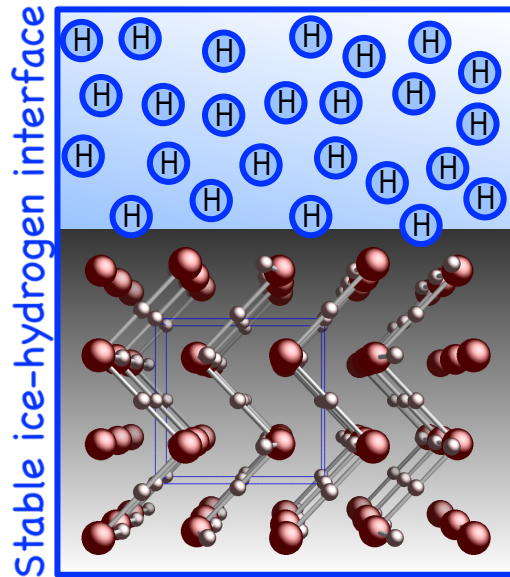
D. Ceperley, R. Cohen, E. de Sturler, J. Kim,
B. Militzer, N. Sobh, and U. Ravaioli.

Why grew the **giant planets** so large while
all **terrestrial planets** stayed small?
Because they form beyond the ice line.



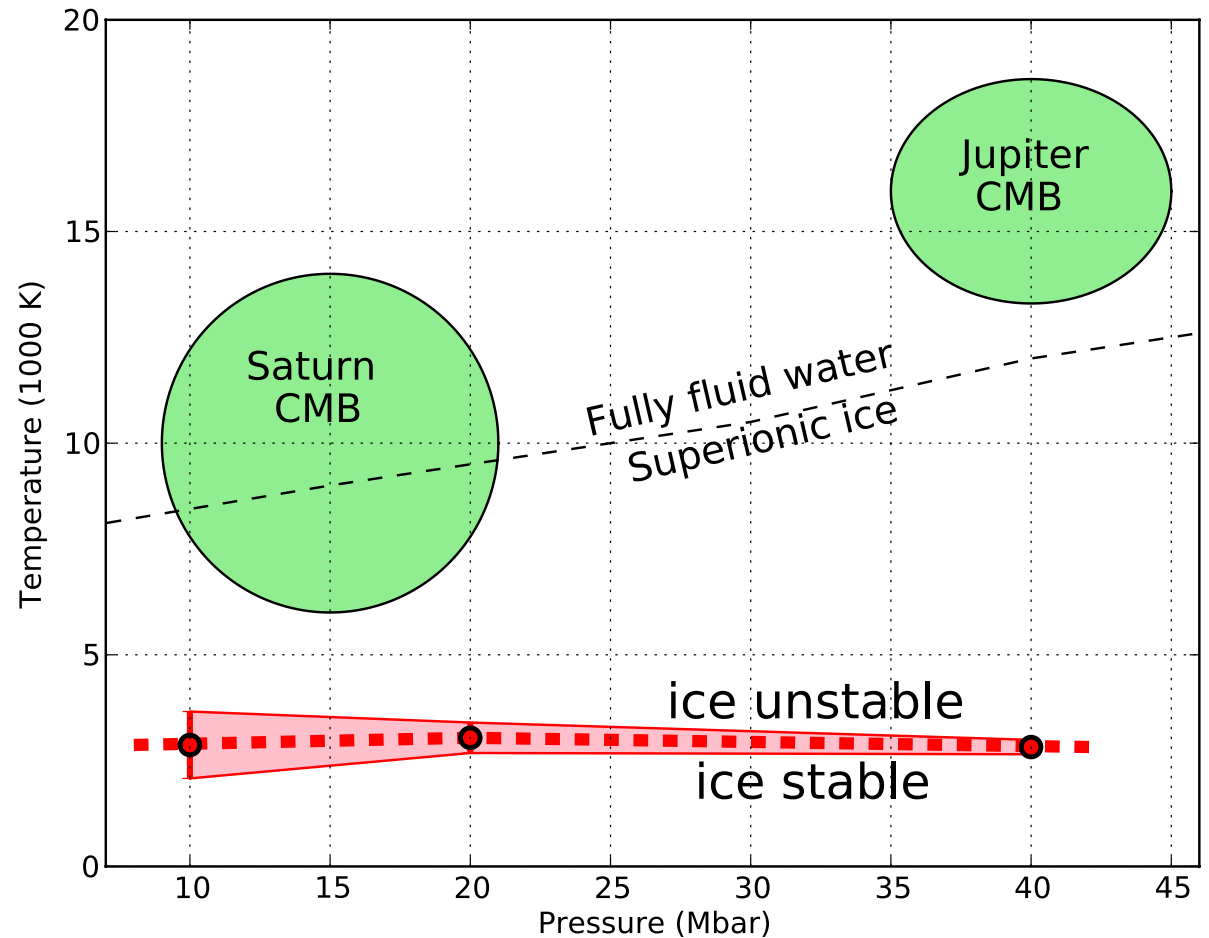
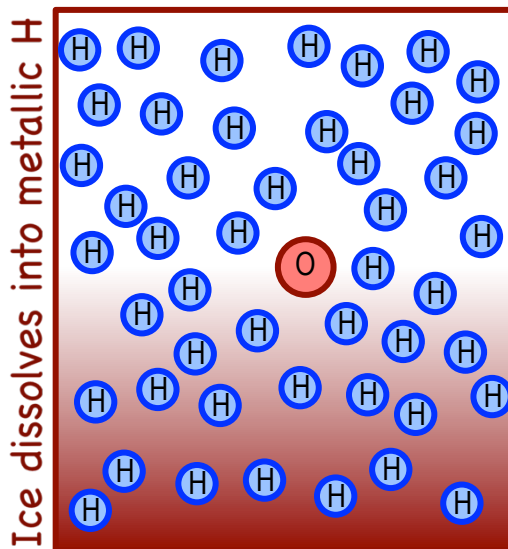
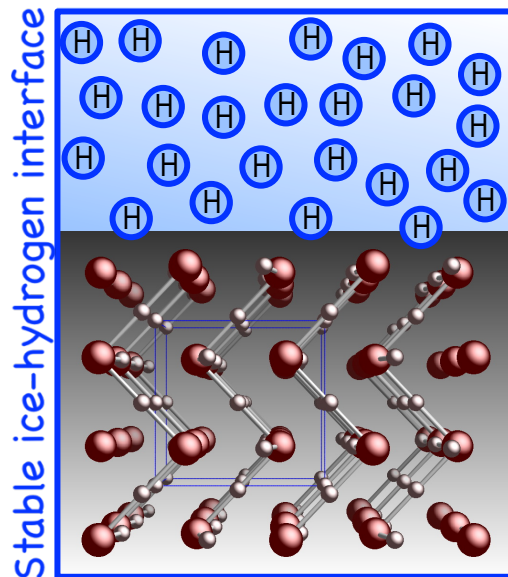
***I. Are the Cores of
Giant Planets Stable?***

Analysis of Gibbs Free Energy differences shows ice erosion is an **entropy driven process**



Predict core erosion in both Saturn and Jupiter
Wilson and Militzer, *Astrophys. J.* 745 (2012) 54

Computer simulations predict **erosion of icy cores** in Saturn and Jupiter

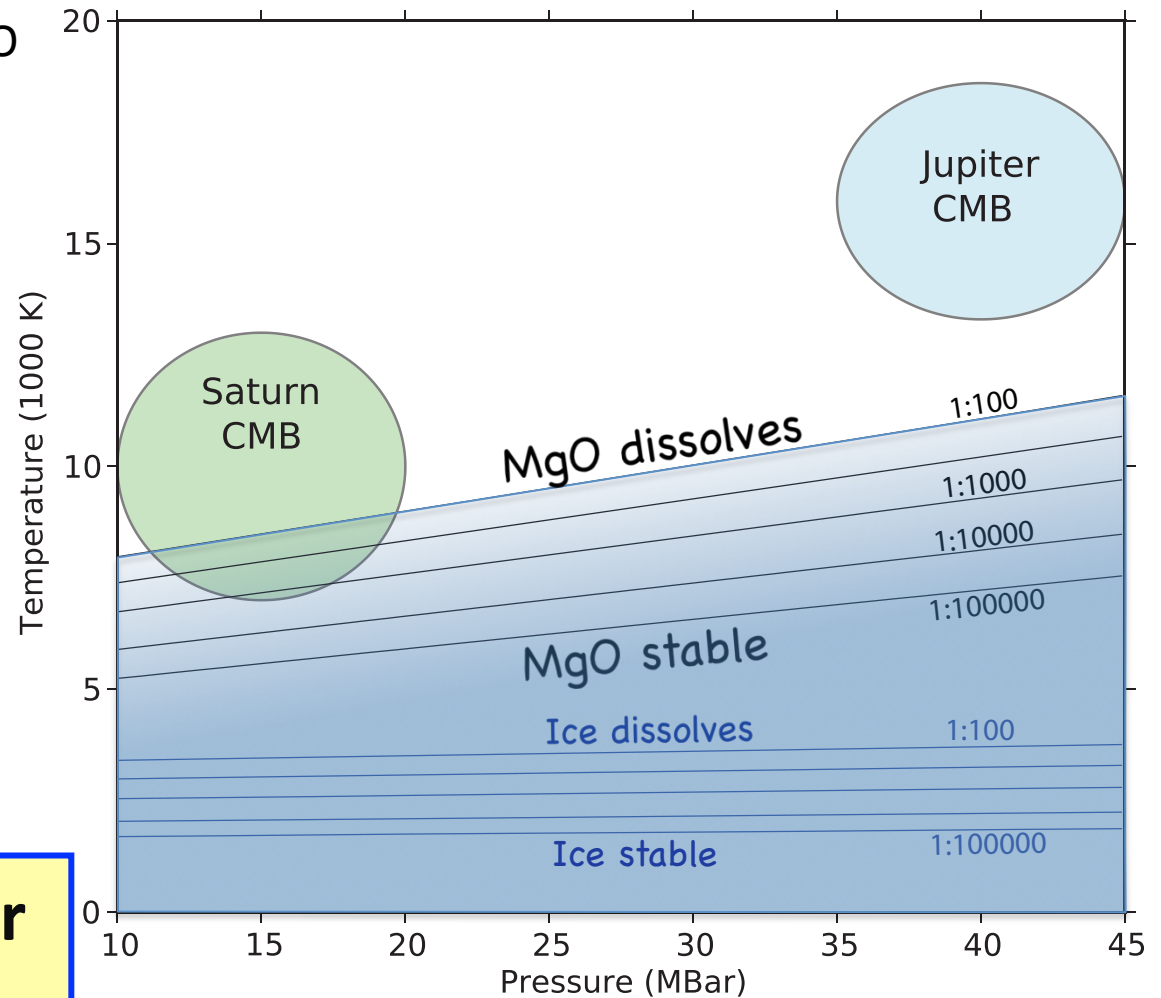
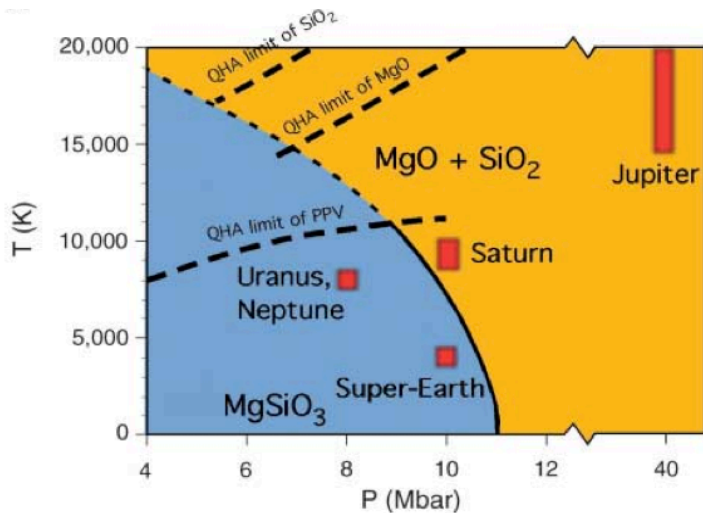


Predict core erosion in both Saturn and Jupiter

Wilson, Militzer, *Astrophys. J.* 745 (2012) 54

Erosion of other core materials: silicates and iron

MgSiO_3 dissociates into SiO_2 and MgO at 11 Mbar (Umemoto, 2006):



MgO dissolves in Jupiter and hot exoplanets but maybe not in Saturn.

Wilson, Militzer, Phys. Rev. Lett. (2012)

Implications of our Core-Erosion Calculations for Jupiter and Saturn

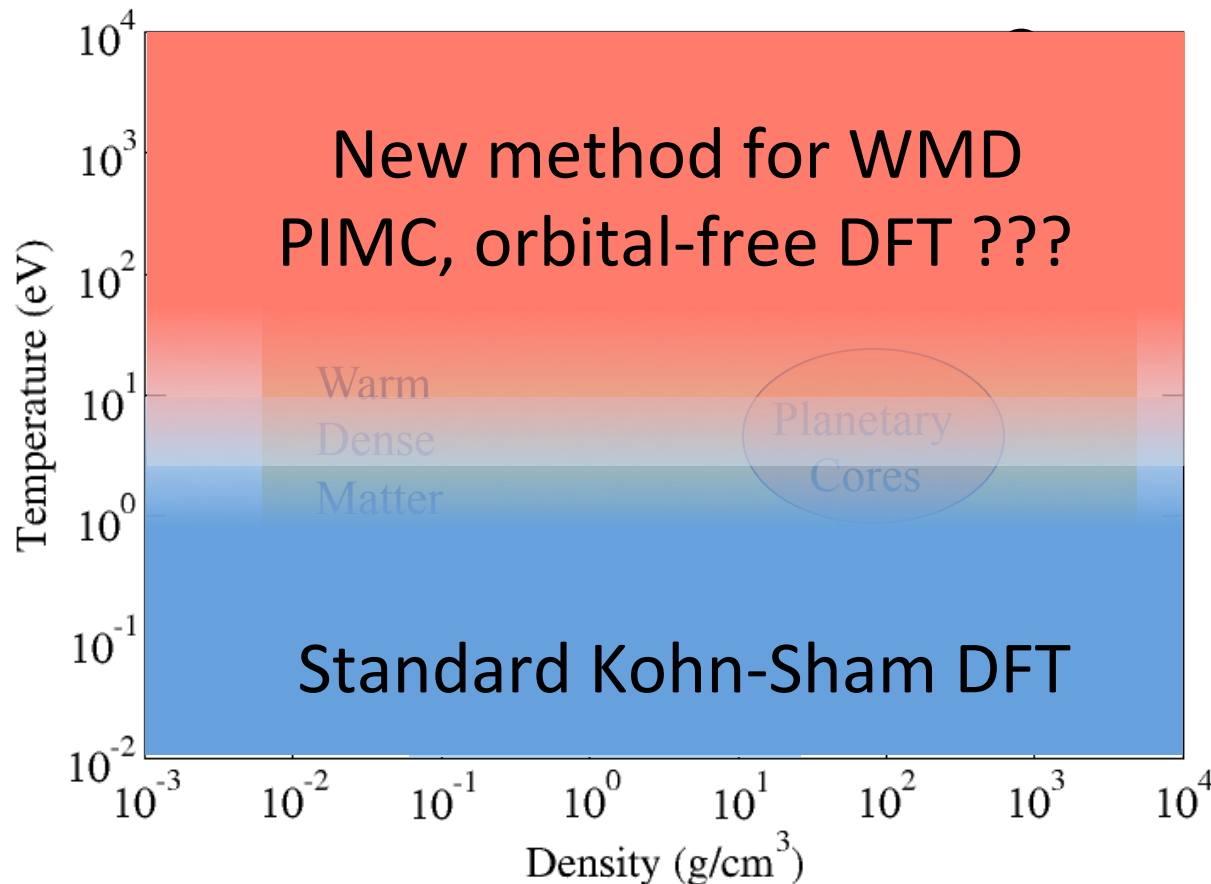
Three core-erosion scenarios:

- **Rapid in Jupiter and Saturn:** homogenized envelopes, core were much bigger originally
- **Slow in J & S:** inefficient up-convection, gravity wins, Juno cannot distinguish a slowly eroding core and a stable one
- **Fast in J, slow in S:** This could explain the difference in core size in the Guillot models for J and S.

Recent core erosion model using double-diffusive convection:
Leconte and Chabrier, A&A (2012)

II. Warm Dense Matter Simulations

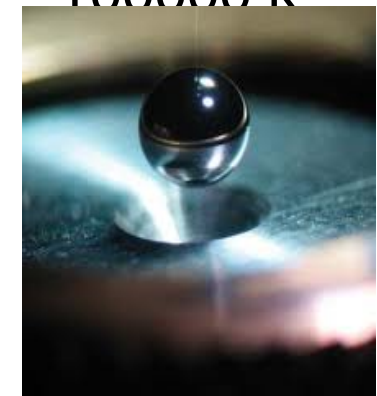
Regime of Warm Dense Matter requires new simulation techniques – Application ICF experiments



ICF Hohlräum

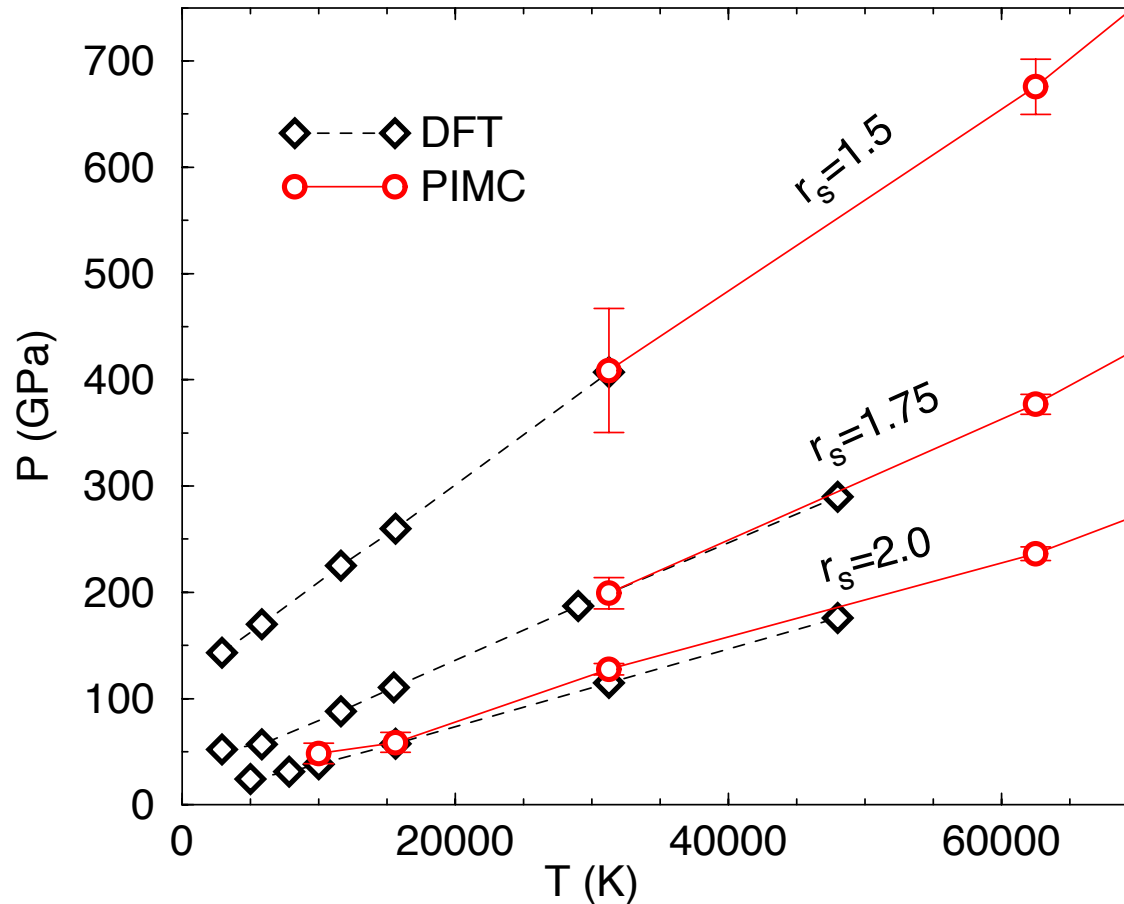


ICF Capsule



Effects of bonding, ionization, exchange and correlation, and quantum degeneracy all important. Carbon is a promising ablator for Inertial confinement fusion (ICF). We are working with LLNL on carbon EOS.

For hydrogen, **PIMC** and **DFT-MD** Simulations Predict Consistent Shock Properties



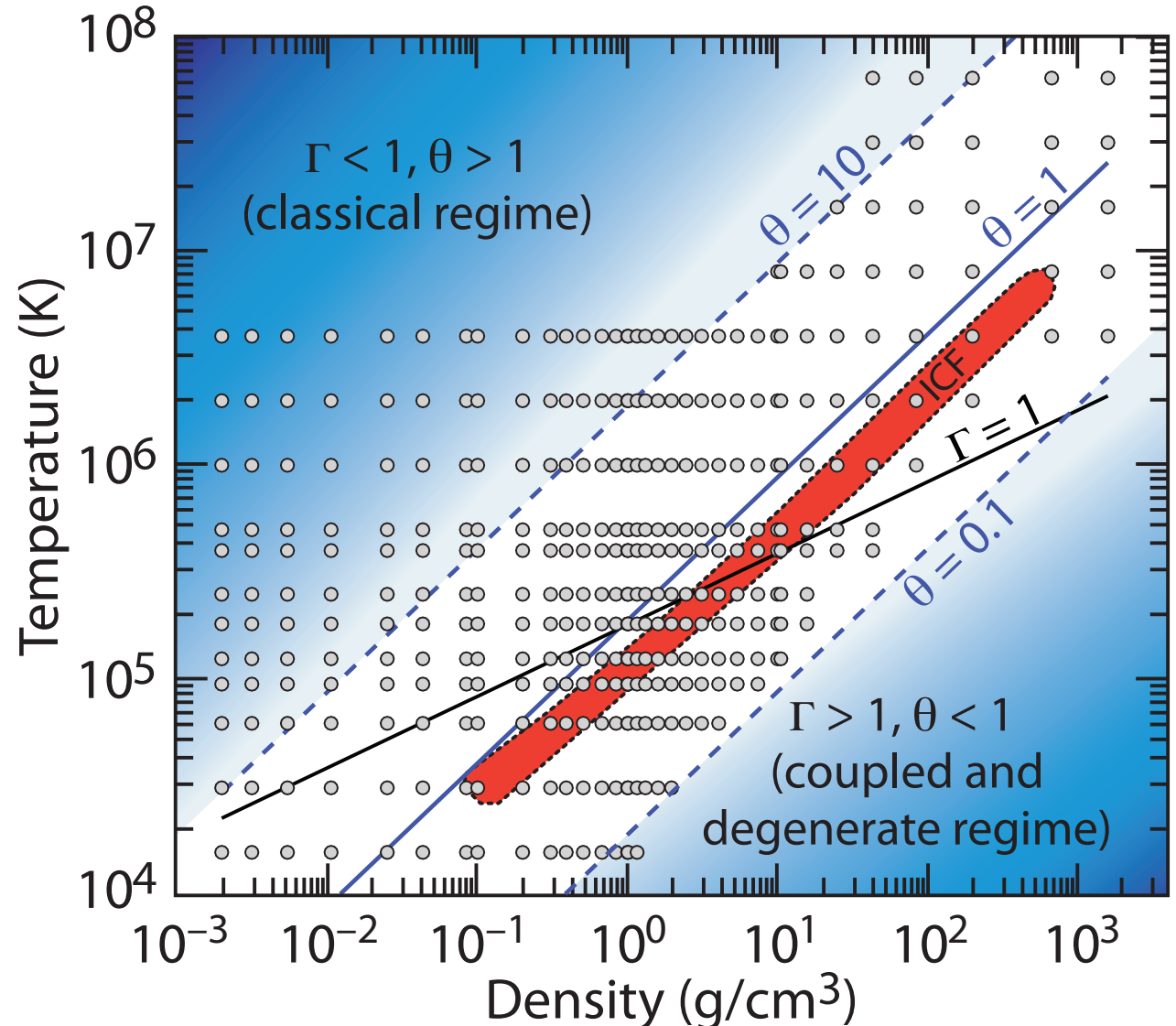
B. Militzer, D. M. Ceperley, J. D. Kress, J. D. Johnson, L. A. Collins, S. Mazevet,
Phys. Rev. Lett. **87** (2001) 275502

Recent **PIMC** work provides EOS for ICF conditions (**FPEOS** table constructed)

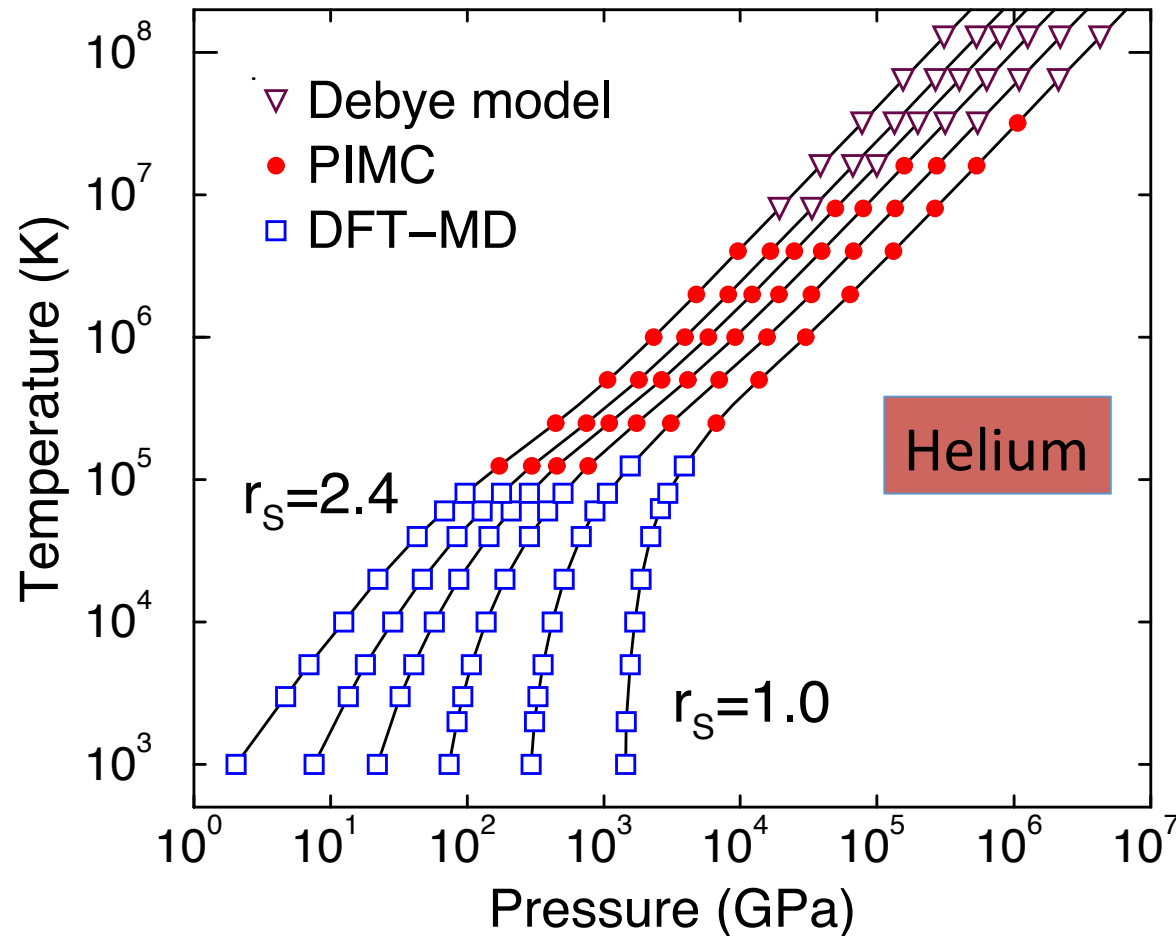
Hydrogen

S. X. Hu, B. Militzer, V. N. Goncharov, S. Skupsky,
Phys. Rev. Lett., **104**
(2010) 235003

Phys. Rev. B **84**
(2011) 224109.



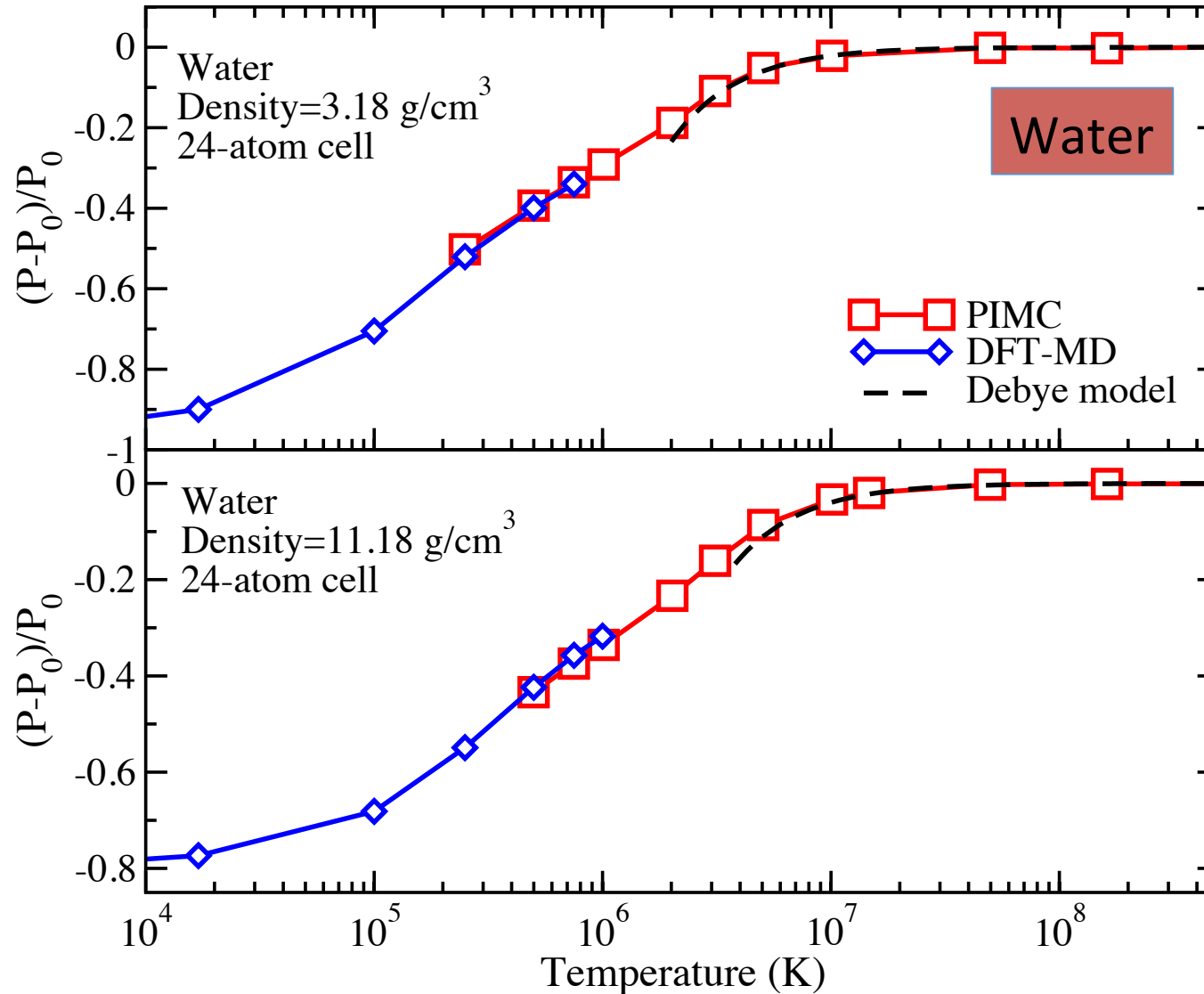
For Helium, **PIMC** and **DFT-MD** Simulations have been combined to make one consistent EOS table



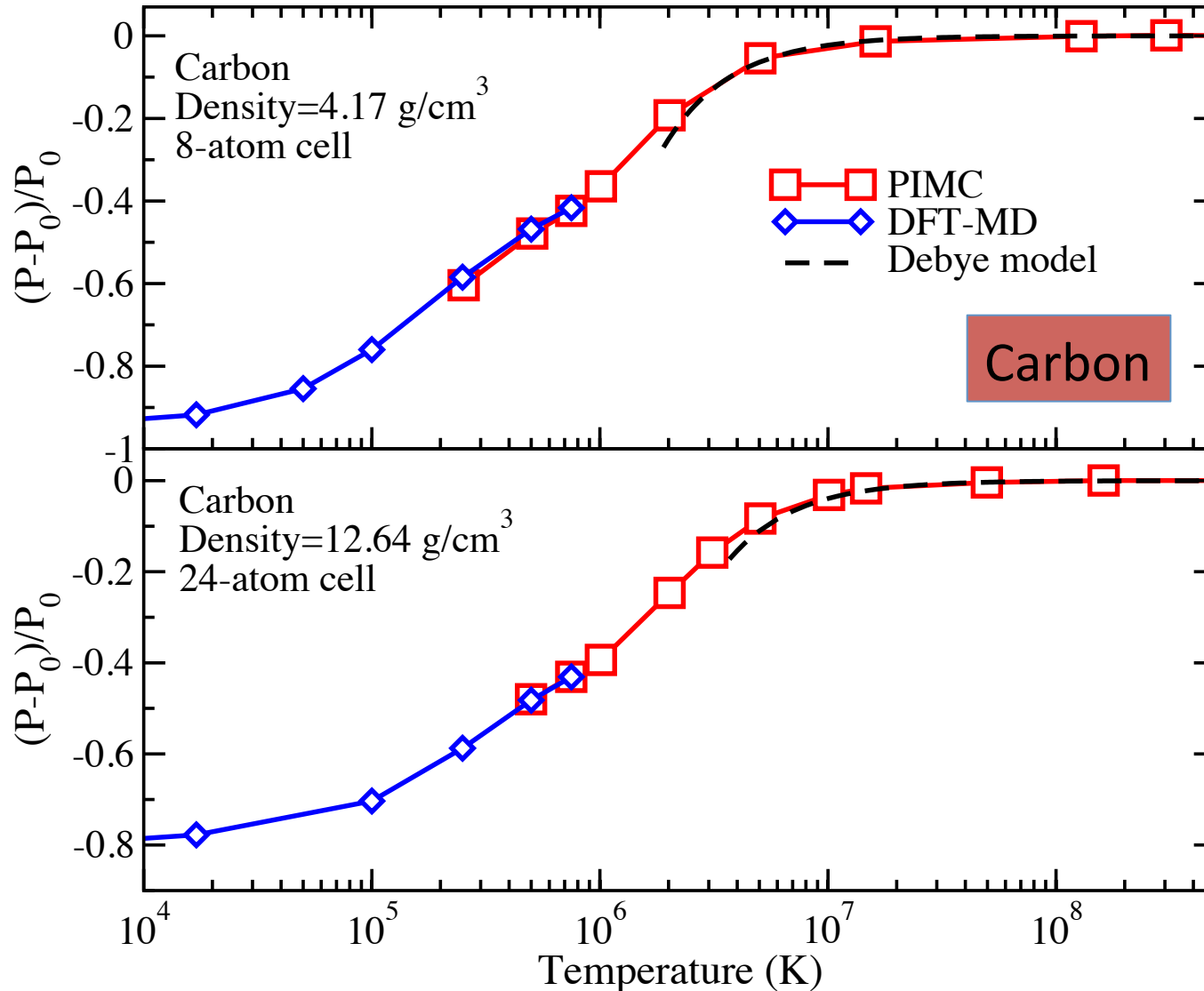
B. Militzer, *Phys. Rev. B* **79** (2009) 155105

B. Militzer, *Phys. Rev. Lett.* **97** (2006) 175501

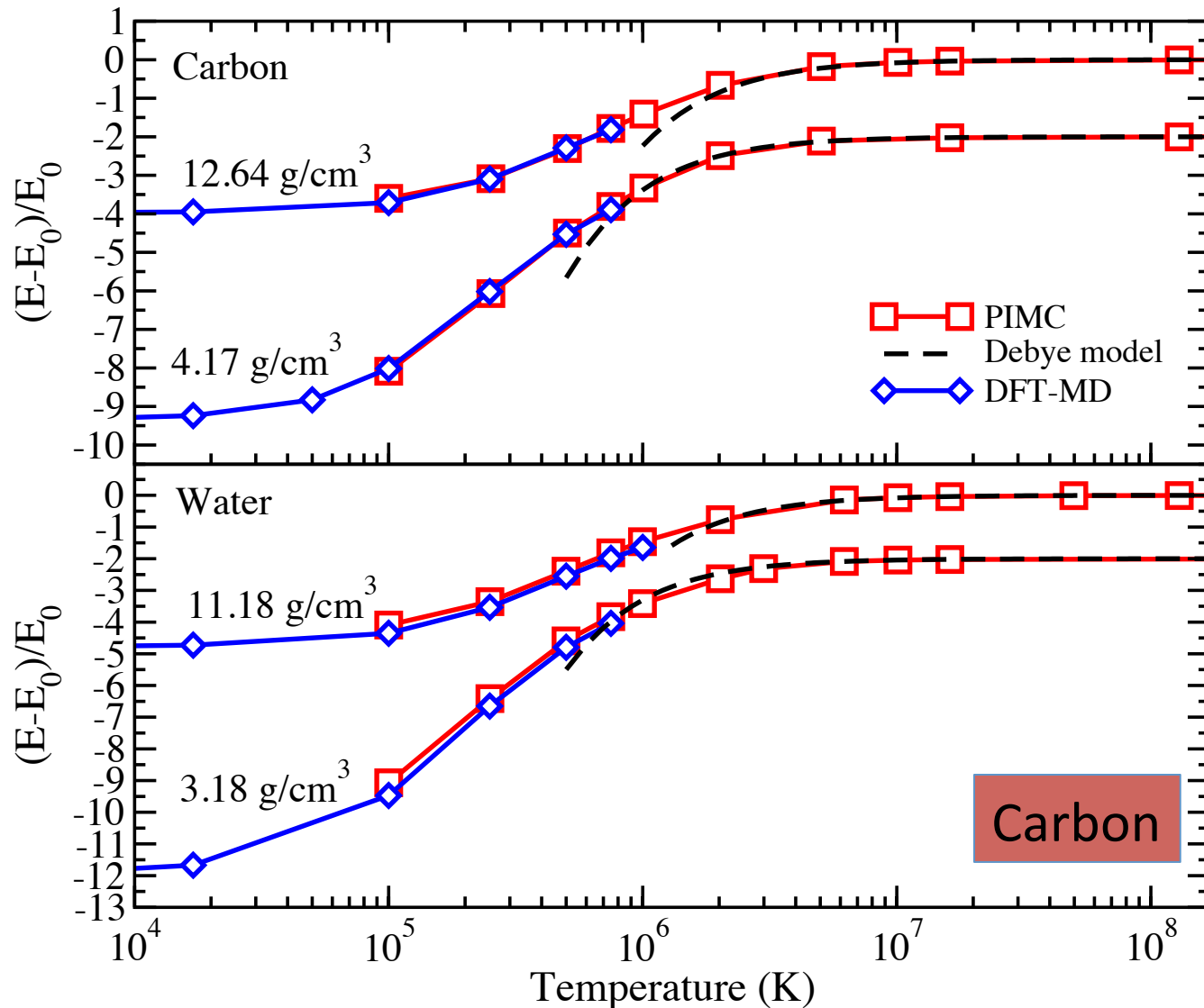
First Path Integral Monte Carlo Simulations for Heavier Elements Fill this Gap in Temperature



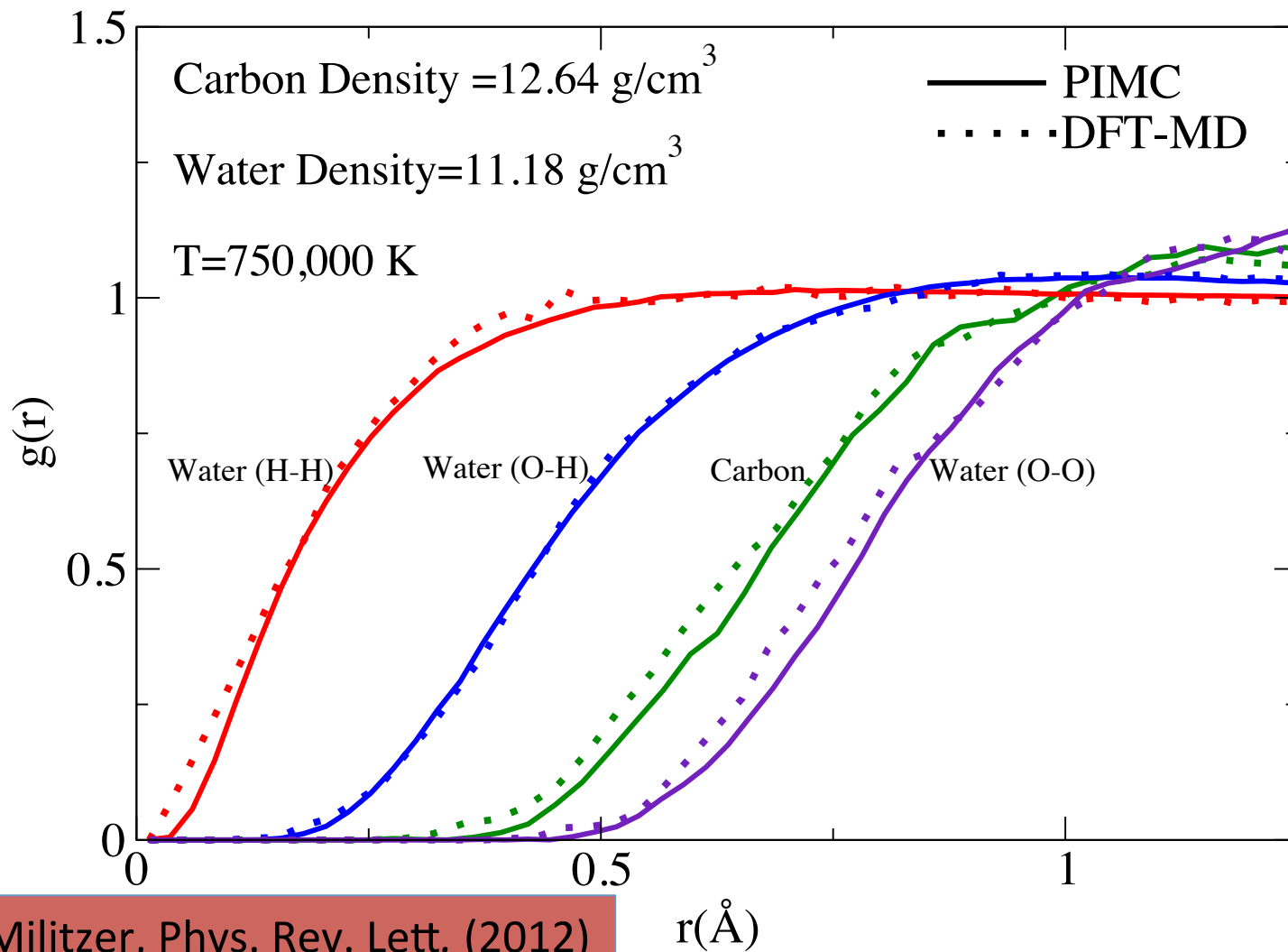
Again **Path Integral Monte Carlo** bridges the Gap in T between DFT-MD and the Debye Model



Path Integral Monte Carlo bridges the Gap in Internal Energy vs Temperature for Water and Carbon Plasmas



Path Integral Monte Carlo and DFT-MD are in very good agreement



Summary

- Presented new **path integral Monte Carlo** simulations for **heavier elements** (all-electron simulations, free particles nodes).
- **Very good agreement with DFT** for **carbon** and **water plasmas**.
- No insufficiencies in the ground-state exchange-correlation functionals.
- We constructed again **consistent EOS table** for C and H₂O.
- **More materials** to be studied. **Please make suggestions!**

Driver, Militzer, Phys. Rev. Lett., 108 (2012) 115502.